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Asymmetric J-curve: Evidence from Industry Trade between U.S. and U.K.

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Previous research that assessed the impact of exchange rate changes on the trade balance between the U.S. and U.K. assumed the effects are symmetric. In this paper we add to the literature on the asymmetric J-curve phenomenon by considering the trade balance of 68 two-digit industries that trade between the two countries. We find short-run asymmetric effects of the real dollar-pound rate in almost all industries. However, short-run asymmetric effects were translated into significant long-run asymmetric effects in 25 industries. Indeed, the asymmetric J-curve hypothesis was supported in 18 industries.

JEL Classification: F31

Key Words: J-Curve, the U.S., U. K., 68 Industries, Asymmetry Analysis

*. Valuable comments of three anonymous referees are greatly appreciated. Any remaining error, however, is ours. Corresponding author: M. Bahmani-Oskooee (bahmani@uwm.edu).

I. Introduction

A country that experiences deterioration in its trade balance may adhere to currency depreciation. However, due to adjustment lags, the effects of a depreciation are not immediate. Indeed, the trade balance still continues to deteriorate and improves only when lags are realized, hence the J-curve pattern. This concept was introduced by Magee (1973) theoretically, and tested by Bahmani-Oskooee (1985) empirically. When researchers found no support for the J-Curve pattern, they suspected aggregation bias in the data. While Rose and Yellen (1989) recommended using aggregate bilateral trade data between two countries, Bahmani-Oskooee and Ardalani (2006) and Bahmani-Oskooee and Wang (2007) emphasized using trade flows between two countries based on commodity-level data.¹

As far as our country of concern, the U.K., is concerned, a few studies have considered the British trade balance with the rest of the world and have reported mixed results. While Miles (1979) found adverse effects of depreciation of the British pound on the U.K.'s trade balance with the rest of the world, Himarios (1989) reported opposite results. However, both studies suffer from the problem of spurious regression, since neither of them engaged in unit root testing nor cointegration analysis. Once Rose (1991), Bahmani-Oskooee and Alse (1994), and Boyd *et al.* (2001) addressed such issues, they found no link between the British trade balance and the value of the pound.

The efforts by Rose and Yellen (1989) and Bahmani-Oskooee and Brooks (1999) to discover some significant link between the trade balance of the U.K. and that of its major partners, especially the U.S., was futile. However, when Bahmani-Oskooee and Kovyryalova (2008) disaggregated trade flows between the U.S. and U.K. by industry, they found significant short-run

¹ Bahmani-Oskooee and Hegerty (2010) is the latest review article on the subject.

effects of the real dollar-pound rate on the trade balance of 107 of 177 industries and favorable long-run effects in 66 of 177 industries, therefore in support of the J-curve effect in 66 industries as well as support for disaggregation by commodity.

All studies reviewed above have assumed that the response of trade balance to exchange rate changes is symmetric, meaning that if $x\%$ depreciation improves the trade balance by $y\%$, then $x\%$ appreciation will worsen the trade balance by $y\%$. However, recent studies argue and demonstrate that the effects of exchange rate changes on the trade balance could be asymmetric. Bussiere (2013) demonstrated that import and export prices react to exchange rate movements in an asymmetric fashion. Bahmani-Oskooee and Fariditavana (2016) then argued that if traded goods' prices respond to exchange rate changes asymmetrically, then so should the trade volumes, and eventually the trade balance. They also argued that an asymmetric response could be due to change in traders' expectations with regards to a depreciation versus an appreciation. Finally, Arize et al. (2017) argued that trade could be subject to hysteresis which implies that if firms do not exit the market during currency appreciation, their export earnings will decline at a different rate than they would increase when currency depreciates, hence asymmetric effects.

The main purpose of this paper is to revisit the trade balance between the U.K. and the U.S. and try to determine the asymmetric response of the trade balance of each of the 68 two-digit industries to changes in the real dollar-pound rate. To that end, we introduce the models and methods in Section II, followed by our empirical results in Section III. A summary is then provided in Section IV, followed by an Appendix in which the sources of the data and definitions of variables are outlined. In order to gain some insight into the movement of the real dollar-pound rate, we plot it over our study period in Figure 1.

Figure 1 goes about here

II. The Models and Methods

Since the method (conducted by prior research) of assessing the symmetric effects of exchange rate changes on trade balance relied upon a reduced-form trade balance model, asymmetry analysis has followed the same path. As such, in both approaches researchers have identified the level of economic activity in each of two trading partners and the real bilateral exchange rate as three main determinants of the trade balance. The theoretical model developed by Rose and Yellen (1989), and conformed to commodity-level data by Bahmani-Oskooee and Kovyryalova (2008), is adopted here as follows:

$$\ln TB_{i,t} = a + b \ln Y_{US,t} + c \ln Y_{UK,t} + d \ln REX_t + \varepsilon \quad (1)$$

Since the data-reporting country is the U.S., equation (1) is from the U.S. perspective. As such, TB_i is defined as the U.S. trade balance of industry i . For sign consistency, we define it as the U.S. imports of commodity i from the U.K. over the U.S. exports of commodity i to the U.K. Defining the trade balance as a ratio enables us to specify the model in logarithmic form. Furthermore, the ratio is unit free (Bahmani-Oskooee 1991). Since an increase in the level of economic activity (Y_{US} and Y_{UK}) stimulates a country's imports, we expect an estimate of b to be positive and that of c to be negative.² As the Appendix reveals, the real exchange rate, REX , is defined such that a decline reflects a real depreciation of the dollar, and if a real depreciation is to improve the trade balance of industry i (i.e., decrease its imports and increase its exports), an estimate of d is expected to be positive.

² Note that if economic growth is due to an increase in production of import-substitute goods, it is possible for an estimate of b to be negative and that of c to be positive since imports will decline as each economy grows (Bahmani-Oskooee 1986).

The estimates discussed above are long-run estimates. In order to also assess the short-run effects of all exogenous variables, the next step is to express (1) in an error-correction modeling format as follows:

$$\begin{aligned} \Delta LnTB_{i,t} = & \alpha + \sum_{j=1}^n \beta_{t-j} \Delta LnTB_{i,t-j} + \sum_{j=0}^n \delta_{t-j} \Delta LnY_{US,t-j} + \sum_{j=0}^n \gamma_{t-j} \Delta LnY_{UK,t-j} + \sum_{j=0}^n \pi_{t-j} \Delta LnREX_{t-j} \\ & + \lambda_1 LnTB_{i,t-1} + \lambda_2 LnY_{US,t-1} + \lambda_3 LnY_{UK,t-1} + \lambda_4 LnREX_{t-1} + \mu_t \end{aligned} \quad (2)$$

Error-correction models such as (2) are introduced by Pesaran et al. (2001), with an advantage over other methods in that the short-run and the long-run effects are estimated in one step by estimating (2). The short-run effects are reflected in the estimates of coefficients attached to the first-differenced variables and the long-run effects are obtained by normalizing estimates of $\lambda_2 - \lambda_4$ normalized on λ_1 . For the normalized estimates to be meaningful, Pesaran et al. (2001) propose applying the F test to establish joint significance of lagged level variables as a sign of cointegration. However, they show that the F test in this context has a new distribution for which they tabulate new critical values that account for the degree of integration of the variables. Indeed, under this method variables could be a combination of I(0) and I(1) and since these are properties of almost all macro variables, there is no need for pre-unit root testing, which is another advantage of this method.

Estimates from (2) reflect symmetric effects of exogenous variables. Shin et al. (2014) modify (2) so that we can infer asymmetric effects. Following their approach, we first form $\Delta LnREX$ which includes positive changes as a reflection of dollar appreciation and negative changes reflecting dollar depreciation. Then, using the partial sum approach, two new series are generated as follows:

$$POS_t = \sum_{j=1}^t \max(\Delta \ln REX_j, 0), \quad NEG_t = \sum_{j=1}^t \min(\Delta \ln REX_j, 0) \quad (3)$$

where POS_t is the partial sum of positive changes and reflects only dollar appreciation. By the same token, the NEG_t variable is the partial sum of negative changes and reflects only dollar depreciation.³ Once the $\ln REX$ is replaced by the two partial sum variables, we have:

$$\begin{aligned} \Delta \ln TB_{i,t} = & a' + \sum_{j=1}^{n1} b'_j \Delta \ln TB_{i,t-j} + \sum_{j=1}^{n2} c'_j \Delta \ln Y_{US,t-j} + \sum_{j=1}^{n3} d'_j \Delta \ln Y_{UK,t-j} \\ & + \sum_{j=0}^{n4} e'_j \Delta POS_{i,t-j} \\ & + \theta_2 \ln Y_{UK,t-1} + \theta_3 POS_{t-1} + \theta_4 NEG_{t-1} + \end{aligned}$$

Since constructing the partial sum variables introduces nonlinearity into (4), it is known as a nonlinear ARDL model, whereas (2) is called a linear ARDL model. Shin et al. (2014) demonstrate that both models are subject to the same estimation procedure and the same diagnostic tests.⁴

Once (4) is estimated, we can test a few asymmetry assumptions. If at any given lag order an estimate of e' is different than the estimate of f' , short-run asymmetric effects of dollar appreciation and dollar depreciation will be recognized. Furthermore, if the Wald test rejects the null of $\sum e' = \sum f'$, short-run cumulative or impact asymmetric effects will be established. On the other hand, long-run asymmetric effects will be recognized if the Wald test rejects the null of

$$\frac{\theta_{-4}}{-\theta_0} = \frac{\theta}{-\theta_0}$$

³ Note that partial sum of positive (negative) changes is the same as cumulative sum where negative (positive) values are replaced by zeros.

⁴ Shin et al. (2014, p. 291) argue that the two partial sum variables should be treated as a single variable so that the critical values of the F test could stay at conservative high level when we move from the linear to nonlinear model.

⁵ For some other application of these and other nonlinear models see Delatte and Lopez-Villavicencio (2012), Bussiere (2013), Wimanda (2014), McFarlane et al. (2014), Gogas and Pragidis (2015), Durmaz (2015), Baghestani and Kherfi (2015), Al-Shayeb and Hatemi-J. (2016), Lima et al. (2016), Aftab et al. (2017), Gregoriou (2017), Nusair (2017), Olaniyi (2019), and Istiak and Alam (2019).

III. Empirical Results

Since the late 1990s, the U.S. has begun reporting its trade statistics on a monthly basis and researchers have begun estimating their models using monthly data. Therefore, we estimate both the linear model (2) and the nonlinear model (4) for each of the 68 two-digit industries that trade between the U.S. and U.K. using monthly data over the period of January 1996 – April 2018. Since the data is monthly, in each model we impose a maximum of 10 lags on each first-differenced variable and use Akaike’s Information Criterion (AIC) to select an optimal model. Since different estimates and diagnostic tests are subject to different critical values, we collect all required critical values in the notes to each table and use them to indicate if an estimate is significant at the 10% or 5% level. We use * to indicate significance at the 10% level and ** at the 5% level. We begin with the estimate of the linear model (2) and report the results in Tables 1-3.

From Table 1, which reports the short-run effects of the real dollar-pound rate, we gather that when the linear model is estimated using aggregate bilateral trade flows (coded by TB in the first row), the real exchange rate carries one significant coefficient. Since the coefficient is negative, dollar depreciation worsens the U.S. trade balance with U.K. in the short-run, consistent with the J-curve hypothesis. It also implies that dollar appreciation improves the trade balance in the short run. Short-run effects, however, do not last into the long-run because the normalized long-run coefficient attached to *LnREX* in Table 2 is insignificant. However, when we consider the estimates for each industry, there are 35 industries in which there is at least one significant lagged coefficient. It appears that some industries even benefit from dollar depreciation since the estimate is positive (e.g. industry coded 00 or 02). Short-run effects last into significant long-run effects in 29 industries (Table 2).

While in 16 industries the normalized long-run coefficient attached to $LnREX$ is positive, in 13 industries it is negative. The 16 industries that will benefit from dollar depreciation in the long run are coded as 00, 01, 02, 03, 04, 05, 22, 28, 55, 58, 63, 78, 81, 87, 88, and 96. While most of these industries are small, one of the largest industries, 78 (Motor vehicles with 10.92% share of trade), is in the list.⁶ Such findings were absent from the estimates of the aggregate bilateral trade balance, which signifies the importance of disaggregation by industry.

The long-run estimates are valid since the F test for cointegration reported in Table 3 is significant. In some cases such as industry 41 (Animal oils and fats) in which the F test is insignificant but the exchange rate carries a significant coefficient, we can rely upon an alternative test known as the t-test or ECM_{t-1} test for cointegration. Under this alternative test, we use normalized long-run coefficient estimates and long-run model (1) and generate the error term. Labeling this error term ECM, we consider the linear error-correction model (2) and replace the linear combination of lagged level variables by ECM_{t-1} and estimate the new specification by imposing the same optimum lags. Cointegration will be supported if ECM_{t-1} carries a significantly negative coefficient.⁷ Indeed, this is the case in most of the optimal models.

A few additional diagnostics are also reported in Table 3. To check for serial correlation and misspecification, we have reported the Lagrange Multiplier test statistic as LM and Ramsey's RESET test as RESET. Since both statistics are insignificant in almost all models, residuals in each optimal model are autocorrelation-free, meaning that these models are correctly specified. We have also applied the well-known CUSUM and CUSUMSQ to the residual of each optimal model to test the

⁶ Note that the 13 industries in which the real bilateral exchange rate carries a negative coefficient are industries for which the import demands are inelastic (Bahmani-Oskooee and Aftab 2017, endnote 11).

⁷ This test originally was introduced by Banerjee et al. (1998) within the Engle-Granger error-correction modeling framework. Pesaran et al. (2001) have incorporated the concept into the ARDL approach, and since we have a combination of $I(0)$ and $I(1)$ variables, as with the F test, they have tabulated new critical values for this t-test which we use in this paper. For cointegration, the calculated t-ratio must be greater than the upper-bound critical values.

stability of short-run and long-run coefficient estimates. Stable estimates are indicated by “S” and unstable ones by “UNS”. Clearly, all estimates are stable. Finally, the size of adjusted R^2 is reported to judge the goodness of the fit in each optimal model.

In order to see how the results change if we consider the estimates of nonlinear models, we report them in Tables 4-7. While the short-run estimates are reported in Tables 4 and 5, long-run estimates are reported in Table 6 followed by diagnostics in Table 7. From Tables 4 and 5 we gather that either ΔPOS or ΔNEG carry at least one significant coefficient in a total of 48 industries, supporting short-run effects of exchange rate changes on the trade balance of these industries. The increase in the number of cases from 35 in Table 1 (short-run estimates of the linear model) to 48 must be attributed to separating dollar appreciation from dollar depreciation and introducing the nonlinear adjustment of the real dollar-pound rate. Furthermore, at a given specific lag order j , the coefficient attached to ΔPOS_{t-j} is different than the one attached to ΔNEG_{t-j} for a majority of the j 's, supporting short-run asymmetric effects of dollar appreciation versus dollar depreciation. However, short-run cumulative or impact asymmetric effects is established only in 25 industries, since the Wald test reported as Wald-S in Table 7 is significant, rejecting the equality of the two sums. These 25 industries are coded as 00, 07, 09, 11, 29, 41, 42, 54, 57, 58, 64, 65, 66, 67, 68, 72, 73, 74, 77, 82, 83, 87, 89, 95, and 97. While many are small industries, several large industries are in the list. They are 11 (Beverages with 2.14% share of trade), 54 (Medical Products with 6.96% trade share), 72 (Machinery Specialized with 2.4% trade share), 74 (General Industrial Machinery with 4.58% trade share), 77 (Electric Machinery with 3.84% trade share), 87 (Professional Scientific Instruments with 3.56% trade share), 89 (Miscellaneous Manufactured Articles with 8.21% trade share), and 97 (Gold, Nonmonetary with 4.56% trade share).

The short-run asymmetric effects last into the long run in 27 industries where, as Table 6 reveals, either the POS or the NEG variable carries a significant coefficient. The estimates are meaningful since either the F test or the ECM_{t-1} test reported in Table 7 is significant, supporting asymmetry cointegration. Although the number of industries that are affected by exchange rate changes in the long run is almost the same as the estimates from the linear models, the nonlinear estimates reveal some interesting information that was masked by the linear models. First, dollar depreciation improves the trade balance of industries coded 00, 05, 11, 28, 55, 56, 58, 63, 64, 66, 73, 81, 84, and 93 since in these 14 industries, the NEG variable carries a significantly positive coefficient. Since total share of trade by these industries is 13.45%, we may conclude that dollar depreciation only helps 13.45% of the trade between the U.S. and the U.K. Second, due to inelastic import demands, dollar depreciation hurts the trade balance of industries coded as 09, 21, 51, 59, 71, 77, and 82 since the NEG variable carries a negative coefficient. The total share of trade by these industries is 13.82%. Thus, dollar depreciation will hurt only 13.82% of the trade between these two countries. It appears that the amount of trade that benefits from dollar depreciation is almost the same as the amount that is hurt. This supports the insignificant coefficient attached to the NEG variable when the linear model is estimated using aggregate bilateral trade flows. Third, dollar appreciation hurts the trade balance of industries coded as 00, 02, 05, 11, 28, 55, 56, 58, 63, 64, 73, 78, 81, 88, 93, and 96 since the POS variable carries a positive coefficient in these industries. These 16 industries engage in a total of 23.46% of the trade. Finally, again due to inelastic import demands, dollar appreciation improves the trade balance of 07, 09, 21, 51, 59, 68, 71, 74, and 77 which altogether engage in 19.12% of the trade. Such findings point at long-run asymmetric effects of dollar depreciation versus dollar appreciation and are supported by the significant Wald test reported as Wald-L in Table 7 in a total of 52 industries.

Putting the industries together from the first group and the third group, the asymmetry J-curve hypothesis introduced by Bahmani-Oskooee and Fariditavana (2016) is supported in a total of 18 industries. The list includes 00, 02, 05, 11, 28, 55, 56, 58, 63, 64, 66, 73, 78, 81, 84, 88, 93, and 96. These are the industries in which both the NEG and POS variables carry a significantly-positive coefficient. Although the nonlinear model did not yield strongly surprising outcomes, it at least identified industries that could benefit from, or be hurt by, changes (in either direction) in the real dollar-pound rate, which could be a good source of information for each industry.⁸

IV. Summary and Conclusion

Since the introduction of asymmetry cointegration and asymmetry error-correction modeling by Shin et al. (2014), the link between the real exchange rate and the trade balance summarized by the J-curve phenomenon has received renewed attention. Indeed, asymmetry analysis, which requires using nonlinear models, separates currency depreciations from appreciations and reveals interesting information that could be masked by symmetry analysis and linear models. While Rose and Yellen (1989) used symmetry analysis and linear models to define the J-curve hypothesis as short-run deterioration combined with long-run improvement, Bahmani-Oskooee and Fariditavana (2016) introduced the concept of asymmetric J-curve in which a depreciation improves the trade balance and an appreciation has no effect, or an appreciation hurts the trade balance and a depreciation has no effect.

In this paper we add to the new literature by considering the trade balance between the U.S. and the U.K.. When we estimated a bilateral trade balance model, we were unable to find any significant link between the two variables either by the linear or nonlinear model. However, when we disaggregated the trade flows between the two countries by industry and estimated both models for

⁸ Note that other diagnostic statistics are similar to those of the linear models and no need to review them again.

each of the 68 two-digit industries, we were able to discover some significant and interesting outcomes. Our findings could be best summarized by saying that when the linear trade balance model was estimated for each industry, we found significant short-run effects of the real dollar-pound rate on the trade balance of 35 industries. Short-run effects lasted into long run significant effects in 29 industries, but only in 16 industries was the symmetry J-curve hypothesis supported. The corresponding numbers were somewhat higher when we estimated the nonlinear models. Indeed, nonlinear models revealed that the exchange rate changes have significant short-run effects on the trade balance of 48 industries. While short-run effects were asymmetric in all industries, short-run cumulative asymmetric effects were established in 25 industries. However, short-run asymmetric effects lasted into significant long-run asymmetric effects in 52 industries.

Since dollar depreciations are separated from dollar appreciations in nonlinear models, additional analysis helped us to identify U.S. industries that benefit from dollar depreciations and those that benefit from dollar appreciations (due to inelastic imports demands). Similarly, we were able to identify industries that are hurt by dollar appreciations and those that benefit from dollar appreciation (again, due to inelastic import demand).

APPENDIX
Data Definition and Source

Monthly data over the period January 1996 - April 2018 are used in the empirical analysis. The data come from the following sources:

- A. US trade online (<https://usatrade.census.gov>)
- B. International Financial statistics (IFS)

Variables:

TB_i = US trade balance with UK for commodity ‘i’ defined as US imports of commodity ‘i’ from UK divided by US exports of commodity ‘i’ to UK [Source:A].

Y_{UK} = UK’s aggregate output as measured by an index of industrial production. [Source:B].

Y_{US} = US aggregate output as measured by an index of industrial production. [Source:B].

REX = The real bilateral exchange rate of the US dollar against Pounds. It is defined as $REX = (P_{US} \cdot NEX / P_{UK})$ where NEX is the nominal exchange rate defined as number of Pound per USD. Thus, a decline in REX reflects a real depreciation of the USD. Both price levels are measured by CPI. All data come from source B.

Figure 1: Plot of the Real Dollar-Pound Rate



Note: A decline reflects a real depreciation of the dollar.

It must be noted that following a referendum on June 2016, the UK government formally announced the country's withdrawal from EU. After the announcement, the pound lost its value against major currencies such as the dollar, as seen in Figure 1. However, since the withdrawal has not been settled, the pound has gained back some of the losses. Could our results be affected by this event? Perhaps not since most of the observations in our study period belong to pre-Brexit referendum period. However, we tested our conjecture by including a dummy in the models to account for this event. Our effort was futile in that the dummy was insignificant, as expected.

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Table 1: Short-Run Coefficient Estimates of Linear ARDL Model (2)

Code	Short-Run Coefficient Estimates									
	$\Delta \text{Ln REX}_t$	$\Delta \text{Ln REX}_{t-1}$	$\Delta \text{Ln REX}_{t-2}$	$\Delta \text{Ln REX}_{t-3}$	$\Delta \text{Ln REX}_{t-4}$	$\Delta \text{Ln REX}_{t-5}$	$\Delta \text{Ln REX}_{t-6}$	$\Delta \text{Ln REX}_{t-7}$	$\Delta \text{Ln REX}_{t-8}$	$\Delta \text{Ln REX}_{t-9}$
TB	-0.67 (2.07)**									
00	1.78(1.84)*									
01	-2.48(1.22)									
02	1.13(2.50)**									
03	0.53(1.97)**									
04	0.91(0.60)									
05	0.45 (1.85)*									
06	-3.87(2.04)**	4.73(2.47)**								
07	-0.37(0.24)	3.38(2.11)**	-1.93(1.20)	0.59(0.36)	3.38(2.10)**					
08	-0.37(0.50)									
09	-2.19(2.47)**									
11	1.56 (1.92)*	-0.56(0.69)	1.91(2.33)**							
12	-1.46(1.50)									
21	-1.08(0.88)									
22	0.12(0.02)									
23	-0.17 (0.53)									
24	0.04(0.07)									
25	10.05(1.64)*	-14.35(2.1)**								
26	0.08(0.25)									
27	-0.34(1.25)									
28	0.94(2.05) **									
29	-2.66 (2.00) **									
32	0.042(0.01)									
33	-1.45(2.08)**									
34	-25.18(0.48)	6.84(0.15)	-53.85(1.14)	16.39(0.38)	25.53(0.48)					
41	-2.18(1.71)*									
42	-0.82(1.17)									
43	-1.36(1.02)									
51	-0.51(1.37)									
52	-1.003(1.60)									
53	-0.068(0.486)									
54	-1.55(1.73)*	-1.07(1.17)	1.80(1.95)*							

55	0.17(1.65)*									
56	0.9(1.186)*									
57	-0.13(1.11)									
58	0.21(2.00)**									
59	-1.65(2.79)**	1.27(2.12)**								
61	0.10(0.42)									
62	-0.07(0.70)									
63	0.66(2.16)**									
64	-1.29(2.35)**									
65	-0.88(2.03)**									
66	0.04(0.18)									
67	-1.84(2.48)**									
68	-0.49(1.54)									
69	-0.033(0.40)									
71	-0.97(1.60)	-1.01(1.64)*								
72	-0.49(0.99)	0.65(1.32)	0.48(0.94)	-1.09(2.16)**						
73	0.33(1.32)									
74	-0.67(2.20)**									
75	-0.72(1.72)*	0.75(1.79)*								
76	0.006(0.05)									
77	-0.21(2.46)**									
78	0.37(1.89)*									
79	-0.19(0.74)									
81	0.62(3.05)**									
82	-0.75(1.26)	-0.83(1.40)								
83	-0.08(0.33)									
84	0.002(0.01)									
85	-1.29(1.05)	-2.68(2.17)**								
87	-0.46(1.45)									
88	-0.57(0.87)	1.08(1.64)*								
89	-0.11(0.57)									
93	0.09(0.42)									
95	4.32(0.94)	-0.06(0.01)	12.36(2.58)**	3.80(0.82)						
96	7.03(2.83)**									
97	-2.93(1.61)									

98	-0.36(1.02)	-0.58(1.63)	0.67(1.88)*	-0.57(1.58)						
99	0.06(0.96)									

Notes: Numbers inside parentheses are absolute values of the t-ratios. The critical value of standard t-ratio is 1.64 (1.96) at the 10% (5%) significance level. * (**) indicate

4 significance at the 10% (5%) level.

Table 2: Long-Run Coefficient Estimates of Linear ARDL Model (2)

<i>Industries</i>	<i>Trade Share</i>	Long-Run Coefficient Estimates			
		<i>Constant</i>	<i>Ln Y_{US}</i>	<i>Ln Y_{UK}</i>	<i>Ln REX</i>
TB (US- UK Trade Balance Aggregate)	100%	-5.85(1.45)	0.47(1.01)	0.76 (1.31)	-0.28(0.96)
00 Live Animals	0.18%	-24.46(2.20)**	-1.14(0.95)	6.54(3.60)**	1.72(1.95)**
01 Meat & Meat Preparations	0.05%	36.68(1.71)*	0.99(0.57)	-8.41(2.27)**	4.70(3.04)**
02 Dairy Products and Birds Eggs	0.08%	20.98(1.98)**	-0.23(0.20)	-3.86(2.42)**	2.21(3.22)**
03 Fish (Except Marine Mammal)	0.22%	4.28(0.45)	3.69(3.87)**	-4.45(2.75)**	1.62(1.96)**
04 Cereals And Cereal Preparation	0.18%	2.45(0.39)	2.47(3.99)**	-2.91(3.07)**	1.074(2.36)**
05 Vegetables and Fruits	0.35%	5.10 (0.80)	1.55(2.20)**	-3.24(3.33)**	0.94(2.21)**
06 Sugars, Sugar Preparations	0.03%	-4.26(0.15)	-11.06(3.76)**	12.16(2.84)**	1.24(0.58)
07 Coffee, Tea, Cocoa	0.09%	-13.40(1.62)	-5.09(5.20)**	7.90(5.92)**	-2.48(3.35)**
08 Feeding Stuff For Animals	0.14%	-90.28(0.74)	12.22(2.57)**	6.65(0.73)	-2.08(0.50)
09 Miscellaneous Edible	0.29%	36.53(8.70)**	-1.97(3.99)**	-6.10(9.75)**	-0.70(2.50)**
11 Beverages	2.14%	8.60(2.71)**	-0.48(1.54)	-1.036(1.96)**	0.34(1.36)
12 Tobacco and Tobacco	0.004%	-51.7(2.14)**	8.31(3.90)**	2.71(0.67)	-2.62(1.40)
21 Hides, Skins and Fur-skins	0.002%	-58.43(2.25)**	2.93(1.11)	9.09(2.17)**	-1.51(0.98)
22 Oil Seeds and Oleaginous	0.10%	-60.89(1.40)	4.39(0.75)	8.27(1.15)	4.25 (1.76)**
23 Crude Rubber	0.07%	24.61(1.17)	-1.74(0.75)	-3.82(1.24)	-0.78(0.54)
24 Cork and Wood	0.56%	-84.59(3.20)**	-7.64(2.96)**	24.75(2.28)**	0.13(0.06)
25 Pulp and Waste Paper	0.01%	-3134.30(0.08)	221.19(0.08)	475.64(0.08)	232.31(0.08)
26 Textile Fibers	0.03%	-50.69(3.13)**	0.88(0.50)	10.08(3.99)**	0.33(0.26)
27 Crude Fertilizers	0.06%	-10.67(1.24)	0.34(0.43)	1.64(1.08)	-0.85(1.14)
28 Metalliferous Ores	1.07%	-11.72(0.70)	-1.15(0.70)	3.67(1.40)	2.81(2.25) **
29 Crude Animal and Vegetable Materials	0.07%	-5.72(1.02)	-1.34(2.47)**	2.29(2.44)**	-0.80(1.80)*
32 Coal, Coke and Briquettes	0.29%	100.73(1.38)	-8.01(0.73)	-14.73(1.33)	0.07(0.01)
33 Petroleum, Petroleum Products	7.57%	-31.11(1.51)	-6.41(2.82)**	13.26(4.20)**	-4.07(2.40)**
34 Gas, Natural and Manufactured	0.30%	143.60(0.43)	-26.07(1.08)	-6.20(0.11)	-13.58(0.78)
41 Animal Oils and Fats	0.02%	-60.61(0.78)	-1.82(0.19)	14.08(1.46)	-9.40(2.07)**
42 Fixed Veg. Fats & Oils	0.01%	-6.73(0.39)	0.57(0.27)	0.78(0.32)	-1.54(1.27)
43 Animal/Veg Fats/Oils Process/Waste	0.02%	16.02(0.18)	-0.71(0.08)	-4.02(0.29)	-8.25(1.03)
51 Organic Chemicals	2.51%	5.56(0.44)	-0.53(0.43)	-0.54(0.26)	-1.39(1.38)
52 Inorganic Chemicals	0.42%	9.44(0.68)	0.69(0.46)	-2.83(1.29)	-2.12(1.77)*
53 Dyeing, Tanning and Coloring Materials	0.24%	-5.87(1.42)	0.023(0.06)	1.27(1.86)*	-0.16(0.47)
54 Medicinal and Pharmaceutical Products	6.96%	-8.18(0.95)	-0.57(0.69)	2.39(1.78)*	-0.34(0.52)

55 Essential Oils	1.28%	-4.70(0.90)	0.11(0.19)	0.91(1.10)	0.76(1.98)**
56 Fertilizers	0.02%	-22.41(2.06)**	2.80(2.64)**	2.17(1.06)	1.17(1.33)
57 Plastics in Primary Form	0.57%	5.30(1.96)**	-0.02(0.08)	-1.22(2.57)**	-0.24(1.10)
58 Plastics in Non-primary Form	0.64%	0.12(0.04)	-0.19(0.52)	0.17(0.34)	0.56(2.55)**
59 Chemical Materials	1.58%	-0.05(0.01)	1.13(2.19)**	-1.15(1.78)**	-0.43(1.26)
61 Leather, Leather MFR	0.04%	-6.71(0.79)	-0.49(0.57)	2.22(1.52)	0.31(0.44)
62 Rubber Manufactures	0.38%	-1.59(0.10)	-0.65(0.41)	1.06(0.46)	-0.65(0.60)
63 Cork and Wood Manufactures	0.09%	-45.89(6.06)**	0.17(0.22)	9.37(8.26)**	1.48(2.42)**
64 Paper, Paperboard	0.52%	-19.94(5.15)**	-0.11(0.26)	4.40(7.17)**	0.30(1.02)
65 Textile Yarn, Fabrics	0.44%	-15.26(3.01)**	0.91(1.62)	2.36(3.00)**	-0.30(0.76)
66 Nonmetallic Mineral	1.13%	-0.82(0.04)	-4.99(2.60)**	5.13(1.77)*	0.24(0.18)
67 Iron and Steel	0.59%	-0.99(0.16)	-0.02(0.03)	0.39(0.39)	-0.87(1.87)*
68 Nonferrous Metals	1.40%	-26.46(2.55)**	2.17(1.84)*	3.47(2.13)**	-1.26(1.75)*
69 Manufactures of Metals	1.45%	-2.23(1.34)	-0.66(3.83)**	1.07(3.90)**	-0.057(0.41)
71 Power Generating Machinery	4.83%	9.13(1.31)	1.77(2.48)**	-3.67(3.29)**	-0.97(2.09)**
72 Machinery Specialised	2.40%	10.52(1.50)	0.52(0.70)	-2.74(2.66)**	-0.19(0.30)
73 Metalworking Machinery	0.28%	-1.86(0.22)	-0.68(0.86)	1.158837	0.95(1.39)
74 General Industrial Machinery	5.58%	3.41(0.72)	-0.25(0.438)	-0.50(0.75)	-0.52(1.49)
75 Office Machines and ADP Equipment	1.47%	-1.01(0.25)	-1.26(3.11)**	1.29(1.92)**	0.26(0.89)
76 Telecommunications Equipment	1.64%	-10.10(3.17)**	1.16(3.32)**	0.87(1.69)*	0.014(0.05)
77 Electrical Machinery, Apparatus & Appliances	3.84%	5.87(1.87)*	1.24(4.05)**	-2.64(5.02)**	-0.63(2.54)**
78 Motor Vehicles	10.92%	-12.25(1.88)*	0.80(1.18)	2.19(2.12)**	0.98(1.88)*
79 Transport Equipment	10.64%	-2.58(0.43)	-1.95(2.43)**	2.16(2.53)**	-0.34(0.86)
81 Prefab Buildings; Sanitary, Plumbing, etc.	0.11%	-1.56(0.53)	1.33(4.34)**	-0.96(2.06)**	0.72(3.35)**
82 Furniture & Bedding	0.77%	15.19(2.73)**	2.09(3.74)**	-5.16(5.54)**	0.14(0.33)
83 Travel Goods, Handbags	0.04%	-4.34(0.42)	0.22(0.19)	0.56(0.35)	-0.25(0.33)
84 Articles of Apparel and Clothing	0.39%	-39.01(3.91)**	-3.24(2.85)**	11.60(7.75)**	0.01(0.01)
85 Footwear	0.04%	71.63(0.65)	-11.47(1.17)	-4.17(0.24)	-2.98(0.47)
87 Professional Scientific Instruments	3.56%	-2.08(1.26)	1.23(6.91)**	-0.74(2.76)**	0.34(2.94)**
88 Photo Appt, Equipment & Optical Goods	0.65%	35.67(9.99)**	-0.80(2.14)**	-6.87(12.65)**	0.61(2.53)**
89 Miscellaneous Manufactured Articles	8.21%	-4.73(1.89)**	-0.94(3.73)**	1.86(4.60)**	-0.11(0.53)
93 Special Transactions	5.25%	-2.25(0.29)	-1.63(1.43)	2.53(2.21)**	0.24(0.44)
95 Coin Including Gold	0.01%	-0.44(0.03)	-4.55(2.73)**	4.99(2.40)**	-2.28(2.33)**
96 Coin (Other Than Gold)	0.01%	-119.59(1.88)*	3.15(0.46)	23.95(2.77)**	12.62(4.00)**
97 Gold, Nonmonetary	4.56%	44.61(1.16)	6.20(1.35)	-17.53(2.66)**	-5.41(1.81)*

98 Estimate of Low Valued Import Transactions	0.40%	-23.45(2.52)**	2.65(2.87)**	6.11(4.15)**	-1.08(1.73)*
99 Low Value Shipments	1.24%	-14.49(1.13)	-2.12(1.51)	1.33(0.72)	0.84(0.75)

Notes: Numbers inside parentheses are the absolute values of the t-ratios. The critical value of standard t-ratio is 1.64 (1.96) at the 10% (5%) significance level. * indicates significance at the 10% level and ** at the 5% level. Trade share is based on sum of imports and exports in the year 2018.

Table 3: Diagnostic Statistics Associated with Linear ARDL Model (2)

Industries	Diagnostics						
	<i>F</i>	<i>ECM_{t-1}</i>	<i>LM</i>	<i>RESET</i>	<i>CUSUM</i>	<i>CUSUMSQ</i>	<i>Adj. R²</i>
TB (US- UK Trade Balance Aggregate)	3.487*	-0.25 (4.20)**	4.76	1.450	S	S	0.464
00 Live Animals	55.93***	-1.03(16.37)***	3.05	0.588	S	S	0.064
01 Meat And Meant Preparations	5.94**	-0.36(5.50)**	3.21	0.001	S	S	0.610
02 Dairy Products and Birds Eggs	9.75**	-0.51(7.04)**	6.45	2.58	S	S	0.409
03 Fish (Except Marine Mammal)	10.24***	-0.32(7.21)**	3.79	1.21	S	S	0.685
04 Cereals And Cereal Preparation	30.18***	-0.73(12.37)**	2.85	0.93	S	S	0.314
05 Vegetables and Fruits	11.13**	-0.48(7.51)**	4.22	0.71	S	S	0.439
06 Sugars, Sugar Preparations	3.34*	-0.19(4.12)**	4.85	1.39	S	S	0.799
07 Coffee, Tea, Cocoa	11.97**	-0.51(7.79)**	2.87	0.06	S	S	0.683
08 Feeding Stuff For Animals	2.63	-0.18(3.65)**	5.00	1.29	S	S	0.581
09 Miscellaneous Edible	13.72**	-0.55(8.34)**	3.38	0.37	S	S	0.516
11 Beverages	10.21**	-0.69(7.21)**	1.63	1.31	S	S	0.275
12 Tobacco and Tobacco	11.33**	-0.60 (7.59)**	4.90	0.36	S	S	0.346
21 Hides, Skins and Fur-skins	21.61**	-0.71(10.50)**	3.61	0.03	S	S	0.145
22 Oil Seeds and Oleaginous	8.05**	-0.58(6.47)**	1.71	0.49	S	S	0.200
23 Crude Rubber	2.57	-0.21(3.61)**	1.83	1.62	S	S	0.497
24 Cork and Wood	4.24*	-0.324(4.64)**	5.12	0.34	S	S	0.712
25 Pulp and Waste Paper	2.09	-0.022(3.34)**	10.26	3.46	S	S	0.379
26 Textile Fibers	3.380*	-0.23(4.14)**	3.28	0.220	S	S	0.575
27 Crude Fertilizers	5.30**	-0.40(5.19)**	1.48	0.666	S	S	0.254
28 Metalliferous Ores	5.93**	-0.33(5.48)**	4.15	0.779	S	S	0.456
29 Crude Animal and Vegetable Materials	25.837**	-0.66(11.45)**	0.44	1.42	S	S	0.255
32 Coal, Coke and Briquettes	5.657**	-0.63(5.50)**	1.97	0.814	S	S	0.167
33 Petroleum, Petroleum Products	5.321**	-0.36(5.20)**	4.29	2.51	S	S	0.627
34 Gas, Natural and Manufactured	2.969	-0.90(4.34)**	0.11	1.87	S	S	0.116
41 Animal Oils and Fats	1.95	-0.23(3.14)**	4.07	0.07	S	S	0.484
42 Fixed Veg. Fats & Oils	8.14**	-0.53(6.43)**	0.80	0.84	S	S	0.136
43 Animal/Veg Fats/Oils Process/Waste	1.41	-0.16(2.68)**	3.39	0.238	S	S	0.440
51 Organic Chemicals	4.03**	-0.37(4.50)**	1.98	0.915	S	S	0.221
52 Inorganic Chemicals	3.848**	-0.47(4.42)**	1.16	0.293	S	S	0.147
53 Dyeing, Tanning and Coloring Materials	6.862**	-0.43(5.90)**	1.17	1.392	S	S	0.264
54 Medicinal and Pharmaceutical Products	4.747**	-0.33(4.91)**	1.22	0.037	S	S	0.437

55 Essential Oils	2.331	-0.22(3.44)**	0.870	0.984	S	S	0.430
56 Fertilizers	32.874**	-0.77(12.92)**	1.357	1.811	S	S	0.095
57 Plastics in Primary Form	8.317**	-0.55(6.50)**	2.010	0.515	S	S	0.164
58 Plastics in Non-primary Form	4.674**	-0.38(4.71)**	0.279	1.238	S	S	0.238
59 Chemical Materials	5.863**	-0.40(5.46)**	0.409	0.586	S	S	0.401
61 Leather, Leather MFR	4.852**	-0.33(4.96)**	0.089	0.749	S	S	0.321
62 Rubber Manufactures	1.767	-0.11(3.00)**	4.262	0.150	S	S	0.675
63 Cork and Wood Manufactures	6.602**	-0.45(5.79)**	0.356	1.511	S	S	0.547
64 Paper, Paperboard	9.715**	-0.43(7.02)**	1.387	1.734	S	S	0.632
65 Textile Yarn, Fabrics	2.106	-0.24(3.27)**	2.041	0.621	S	S	0.550
66 Nonmetallic Mineral	1.316	-0.16(2.57)**	3.122	3.416	S	S	0.776
67 Iron and Steel	5.298**	-0.35(5.19)**	1.831	1.485	S	S	0.387
68 Nonferrous Metals	4.947**	-0.39(5.01)**	0.165	0.055	S	S	0.319
69 Manufactures of Metals	9.243**	-0.58(6.85)**	1.487	1.010	S	S	0.372
71 Power Generating Machinery	4.012**	-0.26(4.51)**	2.534	1.516	S	S	0.692
72 Machinery Specialised	2.567	-0.22(3.61)**	0.276	0.326	S	S	0.597
73 Metalworking Machinery	4.826**	-0.35(4.95)**	0.784	1.866	S	S	0.340
74 General Industrial Machinery	1.432	-0.20(2.70)**	0.615	0.726	S	S	0.471
75 Office Machines and ADP Equipment	3.774*	-0.31 (4.36)**	3.123	2.199	S	S	0.607
76 Telecommunications Equipment	6.223**	-0.40 (5.62)**	0.078	1.087	S	S	0.385
77 Electrical Machinery, Apparatus & Appliances	4.317**	-0.34(4.68)**	1.842	2.083	S	S	0.738
78 Motor Vehicles	4.178**	-0.38(4.61)**	1.551	0.763	S	S	0.367
79 Transport Equipment	9.608**	-0.58(6.98)**	1.362	1.345	S	S	0.298
81 Prefab Buildings; Sanitary, Plumbing, etc.	39.328**	-0.86(14.13)**	0.964	1.429	S	S	0.226
82 Furniture & Bedding	3.951*	-0.30(4.48)**	0.385	0.546	S	S	0.777
83 Travel Goods, Handbags	3.227*	-0.32(4.05)**	1.204	0.063	S	S	0.287
84 Articles of Apparel and Clothing	3.794*	-0.20(4.39)**	0.348	2.759	S	S	0.921
85 Footwear	0.680	-0.047(1.86)*	0.166	2.544	S	S	0.867
87 Professional Scientific Instruments	8.406**	-0.56(6.53)**	0.789	0.722	S	S	0.605
88 Photo Appt, Equipment & Optical Goods	14.550*	-0.54(8.60)**	3.555	1.080	S	S	0.753
89 Miscellaneous Manufactured Articles	13.300**	-0.98(8.22)**	2.839	1.599	S	S	0.229
93 Special Transactions	2.824	-0.37(3.79)**	0.541	0.711	S	S	0.334
95 Coin Including Gold	40.901**	-0.94(14.42)**	0.654	0.102	S	S	0.141
96 Coin (Other Than Gold)	6.064**	-0.56(5.59)**	0.462	0.757	S	S	0.350
97 Gold, Nonmonetary	7.383**	-0.54(6.13)**	1.348	3.738	S	S	0.228

98 Estimate of Low Valued Import Transactions	4.370**	-0.11(4.71)**	0.781	0.429	S	S	0.900
99 Low Value Shipments	1.302	-0.07(2.57)*	0.720	1.129	S	S	0.798

Notes:

a. The critical value of the F test at the 10% (5%) significance level when there are three exogenous variables (k=3) is 3.77 (4.35). These come from Pesaran *et al.* (2001, Table CI-Case III, page 300). *

(**) indicates a significant statistic at the 10% (5%) level.

b. Number inside the parenthesis next to ECM_{t-1} is the absolute value of the t-ratio, Its upper bound critical value is -3.46 (-3.78) at the 10% (5%) significance level and this comes from Pesaran et al. (2001, 7 Table CII-Case III, page 303).

c. LM is the Lagrange Multiplier test of residual serial correlation. It is distributed as χ^2 with 12 degrees of freedom. Its critical value at the 10% (5%) level is 18.55 (21.03).

d. RESET is Ramsey's test for misspecification. It is distributed as χ^2 with one degree of freedom and its critical value at 10% (5%) level is 2.71 (3.84).

e. Abbreviation n.e.s. stands for not elsewhere specified.

Table 4: Short-Run Coefficient Estimates of USD Appreciation in the Nonlinear ARDL Model (3)

Code	ΔPOS_t	ΔPOS_{t-1}	ΔPOS_{t-2}	ΔPOS_{t-3}	ΔPOS_{t-4}	ΔPOS_{t-5}	ΔPOS_{t-6}	ΔPOS_{t-7}	ΔPOS_{t-8}
TB	-0.02 (0.25)								
00	2.02(1.90)**								
01	-7.99(2.30)	3.59(1.02)	3.36(0.93)	3.45(0.96)	-4.46(-1.26)	10.13(3.12)			
02	-2.28(0.72)	3.73(1.20)	-0.10(0.03)	-8.27(2.63)**	-5.77(1.80)*				
03	0.32(1.15)								
04	0.61(1.64)*								
05	0.56 (2.10)**								
06	-4.21(1.13)								
07	1.14(0.46)	5.49(2.18)**	-3.51(1.40)	0.37(0.14)	5.73(2.27)**				
08	-0.60(0.72)								
09	-3.22(2.33)**								
11	0.39(1.93)*								
12	-1.35(1.25)								
21	-2.65(2.03)**								
22	7.92(0.43)	43.50(2.31)**	60.05(2.48)**	16.38(1.05)	17.33(0.95)				
23	-0.51(1.46)								
24	0.06(0.09)								
25	13.55(1.49)	-31.20(3.04)**							
26	0.33(0.94)								
27	1.84(0.98)	2.88(1.51)							
28	-4.25(1.32)								
29	-0.23(0.67)								
32	-496.50(4.1)**	-423.61(3.00)**	-276.05(3.1)**						
33	9.89(2.12)**								
34	-4.09(0.09)	-38.31(0.71)	44.23(0.81)						
41	-7.22(0.94)	4.38(0.56)	-13.16(1.67)*	11.95(1.54)	-19.93(2.57)**				
42	-2.83(0.54)	9.84(1.91)*	3.40(0.69)	-6.37(1.29)	10.97(2.20)**				
43	-1.53(1.15)								
51	-1.72(0.63)	7.6917(2.78)**							
52	-0.86(1.31)								
53	-0.14(0.90)								
54	2.18(1.46)								
55	0.33(2.55)**								

56	-6.94(1.22)	-7.40(1.31)	-8.65(1.50)*						
57	-0.16(1.25)								
58	0.32(2.58)**								
59	-1.83(1.87)*	2.20(2.26)**							
61	-0.08(0.31)								
62	0.02(0.19)								
63	0.86(2.50)**								
64	-1.95(2.30)**								
65	-1.36(2.01)**								
66	0.75(0.52)	0.09(0.06)	-0.52(0.35)	0.33(0.22)	-4.60(3.12)**				
67	-0.24(1.26)								
68	-0.53(1.52)								
69	-0.95(1.69)*								
71	-0.34(1.97)**								
72	-0.02(0.14)								
73	-1.97(1.26)								
74	-1.12(2.31)**	0.63(1.28)							
75	-0.89(1.27)								
76	-0.95(1.27)	-0.10(0.13)	1.86(2.41)**						
77	-0.33(3.24)**								
78	0.37(1.71)*								
79	-2.35(1.33)								
81	0.59(2.67)**								
82	-0.15(1.03)								
83	-1.28(0.76)	-3.37(2.02)**							
84	0.21(1.27)								
85	-3.02(1.60)	-4.67(2.41)**							
87	0.07(0.89)								
88	0.29(1.81)*								
89	0.07(0.32)								
93	0.63(0.46)	-1.68(1.21)	-3.16(2.25)**						
95	9.70(1.35)	1.59(0.22)	19.81(2.71)**	8.02(1.09)					
96	6.20(2.01)**								
97	21.67(1.64)*								
98	-0.10(1.10)								

99	0.08(1.167)								
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Notes: Numbers inside parentheses are the absolute values of the t-ratios.The critical value of standard t-ratio is 1.64 (1.96) at the 10% (5%) significance level. * indicates significance at the 10% leveland ** at the 5% level.

Table 5: Short-Run Coefficient Estimates of USD Depreciation in the Nonlinear ARDL Model (3)

Ind.	ΔNEG_t	ΔNEG_{t-1}	ΔNEG_{t-2}	ΔNEG_{t-3}	ΔNEG_{t-4}	ΔNEG_{t-5}	ΔNEG_{t-6}	ΔNEG_{t-7}	ΔNEG_{t-8}
TB	-1.19(2.04)								
00	16.54(2.23)**								
01	3.15(0.79)	-0.39(0.10)	-1.35(-0.34)	1.77 (0.45)	14.02(3.62)**				
02	2.25(0.63)	2.46(0.68)	-2.01(-0.56)	7.72(2.19)**	5.03(1.44)	6.83(2.08)**			
03	0.003(0.009)								
04	0.49(0.99)								
05	0.71 (2.10)**								
06	-2.43(0.66)	7.15(2.07)**							
07	-0.52(0.98)								
08	-0.88(0.78)								
09	-0.68(2.21)**								
11	0.57(2.10)**								
12	-1.22(0.84)								
21	-5.11(2.85)**								
22	-11.46(0.28)	-99.64(2.91)**	-131.83(3.66)**	-71.29(1.81)*	-95.95(2.91)**	-101.41(3.10)**			
23	3.98(1.63)								
24	0.10 (0.11)								
25	5.27(1.71)*								
26	0.63(1.29)								
27	0.11(0.28)								
28	8.848(2.51)**								
29	-3.58(1.53)	3.50(1.46)							
32	225.89(3.47)**	61.64(1.02)	-75.54(1.37)						
33	-11.22(2.08)**								
34	2.06(0.22)								
41	0.53(0.31)								
42	-6.31(1.08)	-10.26(1.173)*							
43	-2.61(1.57)								
51	3.84(1.24)	-4.68(1.51)							
52	-0.64(0.76)								
53	-0.24(1.168)								
54	-6.48(3.84)**								
55	0.48(2.60)**								

56	13.66(2.15)**	2.14(0.33)	15.09(2.36)**	11.39(1.90)*					
57	-0.21 (1.22)								
58	0.43(2.55)**								
59	-2.06(1.84)*	1.62(1.41)	-1.09(1.01)	2.80(2.61)**	-1.64(1.58)				
61	-0.35(0.99)								
62	0.14(0.84)								
63	1.01(2.22)**								
64	0.50(2.62)**								
65	0.04(0.26)								
66	0.57(1.60)								
67	-2.72(2.08)**								
68	-0.59(1.28)								
69	0.08(0.69)								
71	-2.09(1.94)*	-2.16(1.94)*							
72	-0.58(0.68)	0.61(0.69)	1.08(1.22)	-2.20(2.49)**					
73	0.65(1.73)*								
74	-0.18(1.56)								
75	-0.42(0.51)	1.49(1.95)*							
76	0.06(0.40)								
77	-0.44(3.25)**								
78	0.36(1.28)								
79	0.24(0.62)								
81	0.55(1.89)*								
82	-0.36(1.81)**								
83	0.32(0.86)								
84	0.72(3.08)**								
85	-0.29(0.50)								
87	-0.03(0.33)								
88	0.22(1.00)								
89	0.34(1.26)								
93	2.22(6.81)**								
95	-1.22(0.80)								
96	5.61(1.40)								
97	-19.98(1.35)								
98	-0.88(1.39)	-0.99(1.54)	1.06(1.66)*	-0.85(1.32)	-0.94(1.49)				

99	0.15(1.69)*								
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Notes: Numbers inside parentheses are the absolute value of the t-ratios. The critical value of standard t-ratio is 1.64 (1.96) at the 10% (5%) significance level. * indicates significance at the 10% level and ** at the 5% level.

Table 6: Long-Run Coefficient Estimates of *Nonlinear ARDL Model (3)*

<i>Industries</i>	<i>Trade Share</i>	<i>Constant</i>	<i>Ln Y_{US}</i>	<i>Ln Y_{UK}</i>	<i>POS</i>	<i>NEG</i>
TB (US- UK Trade Balance Aggregate)	100%	-2.17(0.53)	2.10(2.04)**	-1.54(1.16)	-0.07(0.26)	0.25(0.60)
00 Live Animals	0.18%	-18.19(1.57)	0.93(0.30)	3.06(0.78)	1.92(1.94)**	2.39(1.75)*
01 Meat And Mean Preparations	0.05%	28.63(1.22)	-8.79(1.18)	2.10 (0.28)	-0.12(0.03)	-2.27(0.47)
02 Dairy Products and Birds Eggs	0.08%	10.76(1.24)	-7.31(3.31)**	4.94(1.78)*	1.21(1.80)*	-0.12(0.13)
03 Fish (Except Marine Mammal)	0.22%	-6.12(0.62)	-0.71(0.31)	1.80(0.55)	0.92 (1.15)	0.009(0.009)
04 Cereals And Cereal Preparation	0.18%	0.74(0.115)	1.57(1.14)	-1.80(0.94)	0.85 (1.63)	0.67(0.98)
05 Vegetables and Fruits	0.35%	7.62(1.10)	3.00(1.65)*	-5.25(2.17)**	1.16(2.25)**	1.46(1.95)**
06 Sugars, Sugar Preparations	0.03%	6.84(0.28)	-3.79(0.57)	2.79(0.35)	2.58(1.27)	4.00(1.44)
07 Coffee, Tea, Cocoa	0.09%	-4.65(0.63)	-0.74(0.39)	2.11(0.83)	-1.71 (2.37)**	-0.84(0.87)
08 Feeding Stuff For Animals	0.14%	-101.26(1.94)*	4.77(0.38)	16.31(0.96)	-3.17(0.73)	-4.63(0.81)
09 Miscellaneous Edible	0.29%	34.12(7.30)**	-3.42(2.88)**	-4.14(2.56)**	-0.91(2.70)**	-1.21(2.36)**
11 Beverages	2.14%	10.91(3.35)**	0.64(0.88)	-2.64(2.49)**	0.53(2.10)**	0.77(2.36)**
12 Tobacco and Tobacco	0.004%	-48.46(1.78)*	9.55(1.64)*	1.08 (01.2)	-2.42(1.23)	-2.17(0.84)
21 Hides, Skins and Fur-skins	0.002%	-105.14(4.53)**	-12.66(2.00)**	34.07(4.26)**	-3.48(2.13)**	-6.71(2.81)**
22 Oil Seeds and Oleaginous	0.10%	-50.82(1.87)*	23.08(2.13)**	-12.89(0.99)	-2.18(0.81)	-0.29(0.07)
23 Crude Rubber	0.07%	13.89(0.74)	-6.96(1.34)	3.56(0.56)	-2.12(1.40)	-3.17(1.50)
24 Cork and Wood	0.57%	-83.01(2.11)**	-7.06(0.81)	23.84(1.60)	0.18(0.09)	0.30(0.11)
25 Pulp and Waste Paper	0.01%	-1313.99(0.39)	-76.39(0.44)	351.72(0.41)	80.36(0.39)	50.63(0.40)
26 Textile Fibers	0.03%	-38.86(2.36)**	6.42(1.91)*	2.22(0.40)	1.19(0.99)	2.28(1.38)
27 Crude Fertilizers	0.06%	-4.66(0.59)	3.51(1.97)**	-2.58(0.98)	-0.42(0.69)	0.22(0.27)
28 Metalliferous Ores	1.07%	-3.37(0.20)	1.34(0.31)	-0.70(0.13)	3.21(2.20) **	3.79(1.92) *
29 Crude Animal and Vegetable Materials	0.07%	1.54(0.25)	1.75(1.23)	-2.12(1.08)	-0.33(0.69)	0.30(0.47)
32 Coal, Coke and Briquettes	0.29%	-1008.46(0.96)	-149.71(0.69)	363.40(0.86)	49.63(0.87)	9.90(0.38)
33 Petroleum, Petroleum Products	7.57%	-2.70(0.14)	8.77(2.19)**	-6.93(1.10)	-1.98(1.34)	1.04(0.52)
34 Gas, Natural and Manufactured	0.30%	-64.59(0.34)	6.63(0.21)	8.04(0.17)	-0.33(0.05)	2.32(0.25)
41 Animal Oils and Fats	0.02%	-3.94(0.07)	23.23(1.68)*	-20.83(1.53)	-3.16(0.73)	1.76(0.31)
42 Fixed Veg. Fats & Oils	0.01%	-20.02(1.16)	-0.98(0.21)	5.13(0.96)	-2.16(1.45)	-2.67(1.30)
43 Animal/Veg Fats/Oils Process/Waste	0.02%	-72.44(0.59)	-28.66(1.30)	42.33(1.02)	-8.76(1.16)	-14.91(1.61)
51 Organic Chemicals	2.51%	-5.15(0.46)	-5.09(1.97)**	6.20(1.74)*	-2.24(2.64)**	-3.21(2.82)**
52 Inorganic Chemicals	0.42%	15.27(0.97)	2.99(0.88)	-6.06(1.18)	-1.79(1.49)	-1.32(0.88)
53 Dyeing, Tanning and Coloring Materials	0.24%	-8.07(1.95)**	-1.019(1.167)	2.75(2.10)**	-0.29(0.88)	-0.50(1.183)
54 Medicinal and Pharmaceutical Products	6.96%	-8.22(0.85)	0.78(0.38)	1.10(0.36)	-0.14(0.21)	0.09(0.10)
55 Essential Oils	1.28%	-1.57(0.42)	2.46(2.57)**	-2.09(1.73)*	1.01(3.48)**	1.46(3.66)**

56 Fertilizers	0.02%	-8.89(0.727)	4.98(1.62)	-2.77(0.63)	1.52(1.66)*	2.11(1.66)*
57 Plastics in Primary Form	0.57%	4.18(1.38)	-0.43(0.64)	-0.570(0.57)	-0.29(1.25)	-0.37(1.23)
58 Plastics in Non-primary Form	0.64%	1.66(0.60)	1.08(1.46)	-1.44(1.49)	0.73(3.33)**	0.97(3.19)**
59 Chemical Materials	1.58%	-6.75(2.04)**	-2.29(2.29)**	3.58(3.16)**	-0.99(3.39)**	-1.69(4.11)**
61 Leather, Leather MFR	0.04%	-14.46(1.86)*	-4.07(2.23)**	7.26(3.09)**	-0.22(0.30)	-0.96(1.00)
62 Rubber Manufactures	0.38%	1.78(0.15)	3.63(1.62)	-3.69(1.08)	0.15(0.18)	0.92(0.88)
63 Cork and Wood Manufactures	0.09%	-43.30(6.36)**	1.57(1.03)	7.33(3.52)**	1.60(2.86)**	1.88(2.62)**
64 Paper, Paperboard	0.52%	-13.94(3.22)**	2.05(2.21)**	1.04(0.72)	0.59(2.17)**	1.05(2.79)**
65 Textile Yarn, Fabrics	0.44%	-11.80(2.21)**	2.18(1.86)*	0.46(0.28)	-0.12(0.28)	0.15(0.28)
66 Nonmetallic Mineral	1.13%	2.66(0.21)	-0.70(0.24)	0.31(0.08)	1.41(1.61)	2.24(1.89)*
67 Iron and Steel	0.59%	3.44(0.52)	1.85(1.28)	-2.26(1.04)	-0.64(1.40)	-0.26(0.42)
68 Nonferrous Metals	1.40%	-27.25(2.37)**	1.48(0.58)	4.42(1.25)	-1.37(1.76)*	-1.51(1.47)
69 Manufactures of Metals	1.45%	-1.26(0.64)	-0.17(0.41)	0.40(0.63)	0.04(0.29)	0.14(0.72)
71 Power Generating Machinery	4.83%	4.56 (0.63)	0.022(0.01)	-0.96(0.40)	-1.29(2.25)**	-1.67(2.06)**
72 Machinery Specialised	2.40%	11.21(1.28)	1.27(0.65)	-3.59(1.17)	-0.08(0.15)	0.06(0.08)
73 Metalworking Machinery	0.28%	2.26(0.25)	1.27 (0.62)	-1.66(0.53)	1.31(2.02)**	1.72(2.03)**
74 General Industrial Machinery	4.58%	2.19(0.39)	-1.34(1.03)	0.86(0.47)	-0.73(1.97)**	-0.93(1.91)*
75 Office Machines and ADP Equipment	1.47%	1.24(0.28)	-0.43(0.44)	0.008(0.006)	0.42(1.36)	0.60(1.44)
76 Telecommunications Equipment	1.64%	-9.48(2.69)**	1.74(2.20)**	0.18(0.16)	0.05(0.17)	0.16(0.42)
77 Electrical Machinery, Apparatus & Appliances	3.84%	3.11(1.21)	-0.14(0.22)	-0.68(0.87)	-0.81(3.38)**	-1.09(3.43)**
78 Motor Vehicles	10.79%	-12.89(1.78)*	0.71(0.48)	2.31(1.06)	0.96(1.71)*	0.94(1.32)
79 Transport Equipment	10.64%	1.43(0.26)	-0.05(0.03)	-0.46(0.28)	0.013(0.03)	0.40(0.60)
81 Prefab Buildings; Sanitary, Plumbing, etc.	0.11%	-2.44(0.74)	1.10(1.47)	-0.63(0.60)	0.68(2.94)**	0.64(2.03)**
82 Furniture & Bedding	0.77%	9.61(1.90)*	-0.77(0.60)	-1.26(0.72)	-0.40(1.01)	-0.97(1.72)**
83 Travel Goods, Handbags	0.04%	-0.007(0.007)	2.79(1.12)	-2.76(0.86)	0.39(0.52)	0.91(0.92)
84 Articles of Apparel and Clothing	0.39%	-25.59(4.82)**	3.60(2.86)**	2.22(1.37)	0.56(1.28)	1.92(3.24)**
85 Footwear	0.04%	64.69(0.59)	-23.24(0.52)	9.14(0.23)	-4.01(0.34)	-6.14(0.33)
87 Professional Scientific Instruments	3.56%	-3.80(2.22)**	0.33(0.81)	0.45(0.88)	0.12(0.93)	-0.06(0.32)
88 Photo Appt, Equipment & Optical Goods	0.65%	33.65(9.58)**	-1.47(1.65)*	-5.86(5.23)**	0.53(1.94)*	0.39(0.98)
89 Miscellaneous Manufactured Articles	8.21%	-2.72(1.06)	0.30(0.58)	0.26(0.30)	0.06(0.33)	0.30 (1.36)
93 Special Transactions	5.25%	5.37(1.88)*	3.99(7.78)**	-4.48(5.01)**	1.18(5.54)**	2.23(7.82)**
95 Coin Including Gold	0.01%	0.65(0.05)	-0.82(0.22)	1.33(0.32)	-1.94(1.57)	-1.30(0.77)
96 Coin (Other Than Gold)	0.01%	-132.84(1.99)**	-2.11(0.15)	30.49(1.61)	11.13(2.35)**	10.07(1.48)
97 Gold, Nonmonetary	4.56%	137.65(4.58)**	33.40(3.85)**	-62.69(6.54)**	-2.33(0.86)	3.95(1.02)
98 Estimate of Low Valued Import Transactions	0.40%	-22.97(2.30)**	3.65(1.52)	5.12(1.59)	-0.84(1.29)	-0.68(0.74)

99 Low Value Shipments	1.24%	-3.90(0.37)	1.07(0.51)	-4.04(1.22)	0.73(1.01)	1.42(1.41)
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Notes:Numbers inside parentheses are the t-ratios.The critical value of standard t-ratio is 1.64 (1.96) at the 10% (5%) significance level. * indicates significance at the 10% level and ** at the 5% level.

Table 7: Diagnostic Statistics Associated with *Nonlinear* ARDL Model (3)

<i>Industries</i>	<i>F</i>	<i>ECM_{t-1}</i>	<i>LM</i>	<i>RESET</i>	<i>CS (CS²)</i>	<i>Adj. R²</i>	<i>Wald-S</i>	<i>Wald-L</i>
TB (US- UK Trade Balance Aggregate)	3.75**	-0.280(4.79)***	4.765	1.450	(S) (S)	0.472	4.479**	3.994**
00 Live Animals	47.93**	-1.04(17.12)**	4.25	0.457	(S) (S)	0.075	6.548**	3.584**
01 Meat & Meat Preparations	3.67*	-0.26(4.74)**	3.90	2.53	(S) (S)	0.637	0.320	2.950**
02 Dairy Products and Birds Eggs	10.13**	-0.67(7.88)**	2.61	2.13	(S) (S)	0.444	0.383	13.44**
03 Fish (Except Marine Mammal)	9.279**	-0.35(7.53)**	3.03	0.731	(S) (S)	0.689	0.185	23.699**
04 Cereals And Cereal Preparation	24.96**	-0.72 (12.35)**	1.53	1.83	(S) (S)	0.304	0.443	0.742
05 Vegetables and Fruits	9.44**	-0.48(7.60)**	3.68	0.63	(S) (S)	0.439	0.905	1.318
06 Sugars, Sugar Preparations	3.33*	-0.23(3.51)**	3.79	1.36	(S) (S)	0.798	1.057	55.628**
07 Coffee, Tea, Cocoa	10.74**	-0.62(8.11)**	0.834	0.061	(S) (S)	0.692	6.189**	25.970**
08 Feeding Stuff For Animals	2.24	-0.19(3.71)**	4.84	1.24	(S) (S)	0.580	0.591	14.773**
09 Miscellaneous Edible	11.96**	-0.56(8.55)**	3.61	0.205	(S) (S)	0.517	6.384**	5.805**
11 Beverages	12.23**	-0.74(8.65)**	3.65	0.136	(S) (S)	0.255	2.92*	1.553
12 Tobacco and Tobacco	9.42**	-0.55(7.59)**	5.00	0.491	(S) (S)	0.343	0.05	0.03
21 Hides, Skins and Fur-skins	20.33**	-0.76(11.19)**	1.53	1.27	(S) (S)	0.181	1.681	14.86**
22 Oil Seeds and Oleaginous	4.51*	-2.03(6.12)**	2.87	2.28	(S) (S)	0.322	0.034	21.42**
23 Crude Rubber	3.13*	-0.24(4.37)**	3.45	1.53	(S) (S)	0.507	0.278	2.42
24 Cork and Wood	3.52*	-0.33(4.65)**	5.14	0.44	(S) (S)	0.711	0.181	12.638**
25 Pulp and Waste Paper	1.57	-0.10(3.20)**	11.12	5.14	(S) (S)	0.390	0.478	3.04*
26 Textile Fibers	3.181*	-0.27(4.41)**	3.15	0.22	(S) (S)	0.577	0.103	37.78**
27 Crude Fertilizers	8.824**	-0.51(7.34)*	4.04	0.352	(S) (S)	0.265	0.571	10.297**
28 Metalliferous Ores	5.41**	-0.34 (5.76)**	4.18	0.328	(S) (S)	0.464	0.148	4.648**
29 Crude Animal and Vegetable Materials	22.45**	-0.68(11.72)**	1.00	1.46	(S) (S)	0.263	5.716**	7.919**
32 Coal, Coke and Briquettes	4.876**	-0.34(7.08)**	1.49	0.639	(S) (S)	0.496	0.023	0.010
33 Petroleum, Petroleum Products	7.284**	-0.47(6.68)**	1.92	1.682	(S) (S)	0.646	0.032	37.478**
34 Gas, Natural and Manufactured	2.818	-0.89(4.37)**	0.111	0.674	(S) (S)	0.070	0.008	0.230
41 Animal Oils and Fats	2.707	-0.29(4.07)**	1.78	0.866	(S) (S)	0.506	8.336**	43.859**
42 Fixed Veg. Fats & Oils	7.47**	-0.54(6.76)**	1.08	0.792	(S) (S)	0.167	11.741**	3.851**
43 Animal/Veg Fats/Oils Process/Waste	1.438	-0.17(2.97)**	3.70	0.826	(S) (S)	0.442	0.378	9.807**
51 Organic Chemicals	5.344**	-0.47(5.72)**	2.40	1.120	(S) (S)	0.252	0.685	6.901**
52 Inorganic Chemicals	3.270*	-0.48(4.47)**	1.21	0.233	(S) (S)	0.144	0.149	1.681

53 Dyeing, Tanning and Coloring Materials	8.422**	-0.49(7.17)**	1.38	0.886	(S) (S)	0.262	1.334	8.796**
54 Medicinal and Pharmaceutical Products	5.514**	-0.35(5.81)**	1.70	0.206	(S) (S)	0.450	4.584**	0.631
55 Essential Oils	2.646	-0.33(4.02)**	1.214	1.021	(S) (S)	0.437	2.267	59.726**
56 Fertilizers	30.626**	-0.83(13.69)**	2.165	1.074	(S) (S)	0.132	0.021	6.755**
57 Plastics in Primary Form	6.907**	-0.55(6.50)**	4.05	0.198	(S) (S)	0.158	6.467**	0.541
58 Plastics in Non-primary Form	4.118**	-0.44(5.02)**	0.321	1.510	(S) (S)	0.243	5.677**	23.106**
59 Chemical Materials	8.460**	-0.55(7.20)**	1.446	0.361	(S) (S)	0.449	0.602	44.155**
61 Leather, Leather MFR	4.588**	-0.37(5.30)**	0.204	1.022	(S) (S)	0.327	0.791	21.677**
62 Rubber Manufactures	1.918	-0.16(3.43)**	4.279	0.302	(S) (S)	0.677	1.347	49.202**
63 Cork and Wood Manufactures	10.042**	-0.53(7.84)**	1.077	1.295	(S) (S)	0.543	0.932	8.326**
64 Paper, Paperboard	9.399**	-0.48(7.58)**	0.486	1.021	(S) (S)	0.636	12.886**	25.977**
65 Textile Yarn, Fabrics	2.077	-0.25(3.57)**	2.094	0.896	(S) (S)	0.551	4.841**	10.699**
66 Nonmetallic Mineral	1.695	-0.26(3.22)**	3.474	2.062	(S) (S)	0.780	7.529**	23.549**
67 Iron and Steel	5.222**	-0.37(5.65)**	2.254	1.483	(S) (S)	0.388	3.688**	7.899**
68 Nonferrous Metals	4.121**	-0.39(5.02)**	0.150	0.075	(S) (S)	0.316	3.930**	0.050
69 Manufactures of Metals	7.788**	-0.59(6.90)**	3.244	0.513	(S) (S)	0.377	1.139	3.309*
71 Power Generating Machinery	3.943**	-0.27(4.91)**	3.291	1.411	(S) (S)	0.698	0.425	19.444**
72 Machinery Specialised	2.176	-0.22(3.65)**	0.248	0.200	(S) (S)	0.596	3.974**	1.380
73 Metalworking Machinery	4.525**	-0.38(5.26)**	0.451	1.192	(S) (S)	0.344	12.498**	7.327**
74 General Industrial Machinery	1.385	-0.19 (2.91)**	0.588	0.945	(S) (S)	0.472	7.822**	0.134
75 Office Machines and ADP Equipment	3.488*	-0.33(4.62)	2.492	2.250	(S) (S)	0.608	0.037	6.218**
76 Telecommunications Equipment	5.427**	-0.40(5.76)*	0.970	0.557	(S) (S)	0.395	1.861	2.448**
77 Electrical Machinery, Apparatus & Appliances	4.436**	-0.40(5.21)**	2.154	1.729	(S) (S)	0.741	6.553**	20.278**
78 Motor Vehicles	3.468*	-0.38(4.61)**	1.480	0.789	(S) (S)	0.365	0.054	0.833
79 Transport Equipment	8.243**	-0.59(7.10)**	0.439	1.120	(S) (S)	0.302	0.695	4.616**
81 Prefab Buildings; Sanitary, Plumbing, etc.	36.681**	-0.86(14.14)**	0.911	1.495	(S) (S)	0.223	0.632	0.627
82 Furniture & Bedding	4.434**	-0.37(5.21)**	1.492	1.732	(S) (S)	0.779	8.518**	28.915**
83 Travel Goods, Handbags	3.133*	-0.35(4.38)**	1.903	0.783	(S) (S)	0.295	5.643**	9.398**
84 Articles of Apparel and Clothing	9.651**	-0.38(7.68)**	0.301	1.901	(S) (S)	0.924	1.732	141.40**
85 Footwear	1.239	-0.05(2.75)**	0.078	2.478	(S) (S)	0.869	0.246	103.13**
87 Professional Scientific Instruments	9.671**	-0.58(7.69)	0.352	0.309	(S) (S)	0.603	6.539**	16.44**
88 Photo Appt, Equipment & Optical Goods	12.698**	-0.55(8.81)**	0.094	0.571	(S) (S)	0.751	0.713	6.721**

89 Miscellaneous Manufactured Articles	11.500**	-1.15(8.39)**	0.092	0.998	(S) (S)	0.238	8.793**	2.930*
3 Special Transactions	43.843**	-0.99(16.38)**	0.726	1.661	(S) (S) 2	0.397	0.011	59.617**
95 Coin Including Gold	35.015**	-0.94(14.65)**	0.895	0.166	(S) (S)	0.153	5.00**	2.729*
96 Coin (Other Than Gold)	5.058**	-0.56(5.61)**	0.430	1.016	(S) (S)	0.346	0.181	0.092
97 Gold, Nonmonetary	9.863**	-0.71(7.78)**	0.982	2.229	(S) (S)	0.272	3.282*	13.19**
98 Estimate of Low Valued Import Transactions	4.190*	-0.12(5.07)**	0.297	0.609	(S) (S)	0.899	0.120	0.622
99 Low Value Shipments	1.794	-0.11(3.31)**	1.866	1.532	(S) (S)	0.797	1.255	32.16**

Notes: a. The critical value of the F test at the 10% (5%) significance level when there are three exogenous variables (k=3) is 3.77 (4.35). These come from Pesaran *et al.* (2001, Table CI-Case III, page 300). * (**) indicates a significant statistic at the 10% (5%) level.

b. Number inside the parenthesis next to ECM_{t-1} is the absolute value of the t-ratio, Its upper bound critical value is -3.66 (-3.99) at the 10% (5%) significance level and this comes from Pesaran et al. (2001, Table CII-Case III, page 303). Note that these values are for k=4.

is the Lagrange Multiplier test of residual serial correlation. It

RESET is Ramsey's test for misspecification. It is distributed as χ^2

apply to both Wald tests.

APPENDIX
Data Definition and Source

Monthly data over the period January 1996 - April 2018 are used in the empirical analysis. The data come from the following sources:

- A. US trade online (<https://usatrade.census.gov>)
- B. International Financial statistics (IFS)

Variables:

TB_i = US trade balance with UK for commodity ‘i’ defined as US imports of commodity ‘i’ from UK divided by US exports of commodity ‘i’ to UK [Source:A].

Y_{UK} = UK’s aggregate output as measured by an index of industrial production. [Source:B].

Y_{US} = US aggregate output as measured by an index of industrial production. [Source:B].

REX = The real bilateral exchange rate of the US dollar against Pounds. It is defined as $REX = (P_{US} \cdot NEX / P_{UK})$ where NEX is the nominal exchange rate defined as number of Pound per USD. Thus, a decline in REX reflects a real depreciation of the USD. Both price levels are measured by CPI. All data come from source B.

Figure 1: Plot of the Real Dollar-Pound Rate



Note: A decline reflects a real depreciation of the dollar.

It must be noted that following a referendum on June 2016, the UK government formally announced the country's withdrawal from EU. After the announcement, the pound lost its value against major currencies such as the dollar, as seen in Figure 1. However, since the withdrawal has not been settled, the pound has gained back some of the losses. Could our results be affected by this event? Perhaps not since most of the observations in our study period belong to pre-Brexit referendum period. However, we tested our conjecture by including a dummy in the models to account for this event. Our effort was futile in that the dummy was insignificant, as expected.